

`intcensROC`

Fast Spline Based Sieve AUC Estimator for Interval Censored Data

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This document provides an comprehensive example for using the `intcensROC` package to estimate the receiver operating characteristic (ROC) curve and time-dependent area under the curve (AUC) for interval censored survival data, that is not not applicable for existing methods.

The estimator applies a generalized gradient projection method on Spline based likelihood function to obtain the joint distribution function between survival time and biomarker and compute the ROC curve and time-dependent AUC with the estimated joint distribution function. Features of this package include:

- 1 The algorithm is implemented in C++, and ported to R by Rcpp, to facilitate fast computation.
- 2 The estimator uses a constrained minimization method and is designed for the interval survival data.

# Function Signature and Return of `intcensROC`

Function to compute ROC curve

```
res <- intcensROC(U, V, Marker, Delta, PredictTime, gridNumber = 500)
```

Function arguments:

**U:** An array contains left times of the censored intervals for the sample.

**V:** An array contains right times of the censored intervals for the sample.

**Marker:** An array contains marker levels for the samples.

**Delta:** An array of indicator for the censoring type, use 1, 2, 3 for left, interval and right censoring types, correspondingly.

**PredictTime:** A scalar for predict time for the ROC.

**gridNumber:** A integer for the number of grid of the ROC curve, the default value is 500.

Function return:

A dataframe contains two columns

**tp:** A array for true positive rate.

**fp:** A array for false positive rate.

# Function Signature and Return of `intcensAUC`

Function to compute AUC

```
auc <- intcensAUC(ROCdata)
```

Function argument:

`ROCdata`: A dataframe from the function `intcensROC`.

Function return:

`auc`: A scalar for AUC.

# A Simple Start Off Example

A start off example to use function `intcensROC` and `intcensAUC`

```
library(intcensROC)
## example interval censored data
U <- runif(100, min = 0.1, max = 5)
V <- runif(100, min = 0.1, max = 5) + U
Marker <- runif(100, min = 5, max = 10)
Delta <- sample.int(3, size = 100, replace = TRUE)
pTime <- 4
## compute the ROC curve
res <- intcensROC(U, V, Marker, Delta, pTime, gridNumber = 500)
head(res)

##           fp           tp
## 1 2.938704e-07 6.709990e-07
## 2 6.429442e-07 1.401916e-06
## 3 1.102661e-06 2.253220e-06
## 4 1.728461e-06 3.285375e-06
## 5 2.575783e-06 4.558851e-06
## 6 3.700067e-06 6.134114e-06

##compute the AUC
auc <- intcensAUC(res)
print(auc)

## [1] 0.5378973
```

## Example-Background

Here, we present a comprehensive example as a tutorial on how to use `intcensROC` package.

- We assume the survival time  $T$  follows an exponential distribution with hazard rate  $\lambda = \frac{\log(2)}{24}$ .
- The marker  $M$  is assumed to follow a beta distribution with parameter  $\alpha = 2.35$  and  $\beta = 1.87$ .
- The joint distribution of  $(T, M)$  is assumed to be generated by Clayton Coupla with parameter  $\alpha > 1$

$$F_{T,M}(t, m) = Pr(T < t, M < m) = \{F_T(t)^{\alpha-1} + F_M(m)^{\alpha-1} - 1\}^{\frac{1}{\alpha-1}}$$

Here  $F_T(\cdot)$  and  $F_M(\cdot)$  denote the distribution functions of  $T$  and  $M$  respectively. The dependence between  $T$  and  $M$  is denote by Kendall  $\tau = \frac{\alpha-1}{\alpha+1}$

- The random assessment interval  $[U, V]$  are sampled from uniform distribution,  $V$ 's are sampled within  $[L_0, L_c]$ , and  $U$  is generated from uniform distribution on  $[0, V - L_0]$ . Here  $L_c$  is determined by the censoring rate  $\rho = 0.3$  and  $L_0 = 0.1$  is the minimum time difference between  $U$  and  $V$ .

```
library(copula)
f<-function(x,L0,rate,censor){
  1/((x-L0)*rate)*exp(-L0*rate)-1/((x-L0)*rate)*exp(-x*rate)-censor}
dataSim <- function(kendall_tau = 0.3, n = 100, rho = 0.3, lambda = log(2)/6)
{
  b_alpha      <- 2.35
  b_beta       <- 1.87
  scale        <- 10
  kendall_tau  <- iTau( claytonCopula(), kendall_tau)
  Int_cop      <- claytonCopula(param = kendall_tau, dim = 2)
  Int_mvdc     <- mvdc(Int_cop, c("exp","beta"), paramMargins =
    list(list(rate = lambda),
    list(shape1=b_alpha,shape2=b_beta)))
  Int_obs_data <- rMvdc(n, Int_mvdc)
  colnames(Int_obs_data) <- c("event_time", "marker")
}
```



## Data Simulation-Continued

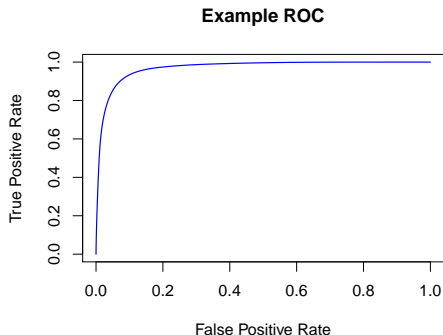
```
Int_obs_data[, "marker"] <- Int_obs_data[, "marker"] * scale
L0      <- 0.1; size      <- n; U      <- rep(0, size)
L       <- uniroot(f, lower = 10-6, upper = 500, tol = 0.000001,
                  L0 = L0, rate = lambda, censor = rho)
V       <- runif(size, L0, L$root)
for (i in 1:size)
  U[i] <- runif(1, 0, (V[i] - L0))
delta_1 <- Int_obs_data[, "event_time"] < U
delta_2 <- Int_obs_data[, "event_time"] >= U &
  Int_obs_data[, "event_time"] <= V
delta_3 <- Int_obs_data[, "event_time"] > V
data    <- data.frame(U = U, V = V, delta =
  delta_1 + 2 * delta_2 + 3 * delta_3,
  marker = Int_obs_data[, "marker"])
}
```

# Compute ROC and AUC

```
mydata <- dataSim(kendall_tau = 0.7, n = 300, rho = 0.3, lambda = log(2)/24)
roc     <- intcensROC(U=mydata[, "U"], V=mydata[, "V"], Marker=mydata[, "marker"],
                     Delta=mydata[, "delta"], PredictTime=12)
print(intcensAUC(roc))
```

```
## [1] 0.9700358
```

```
plot(roc$fp, roc$tp, type = "l", lwd = 1.2, col="blue", main = "Example ROC",
     xlab = "False Positive Rate", ylab = "True Positive Rate" )
```



## Session Information

- R version 3.4.4 (2018-03-15), x86\_64-pc-linux-gnu
- Running under: Debian GNU/Linux 9 (stretch)
- Matrix products: default
- BLAS: /usr/lib/openblas-base/libblas.so.3
- LAPACK: /usr/lib/libopenblas-p-r0.2.19.so
- Base packages: base, datasets, grDevices, graphics, methods, stats, utils
- Other packages: copula 0.999-18, intcensROC 0.1, knitr 1.20
- Loaded via a namespace (and not attached): ADGofTest 0.3, Matrix 1.2-12, Rcpp 0.12.16, compiler 3.4.4, evaluate 0.10.1, grid 3.4.4, gsl 1.9-10.3, highr 0.6, lattice 0.20-35, magrittr 1.5, mvtnorm 1.0-7, numDeriv 2016.8-1, pcaPP 1.9-73, pracma 2.0.7, pspline 1.0-18, quadprog 1.5-5, stabledist 0.7-1, stats4 3.4.4, stringi 1.1.7, stringr 1.3.0, tools 3.4.4

```
## [1] "Start Time Tue May 1 09:44:02 2018"  
## [1] "End Time Tue May 1 09:44:06 2018"
```