

# Birth Data - Loglinear Models

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```
library(catdata)

data(birth)
attach(birth)
```

In the following loglinear models are fitted with the binary variables Sex, Membranes, Cesarean and Induced from the "birth" data. As an overview a contingency table is plotted.

```
table1 <- table(Sex, Membranes, Cesarean, Induced)

ftable(table1)
```

Now we start fitting the models. The goal is to find a model with good fit but sparse parametrization.

First the saturated model is fitted, then the model with all 3-factor interactions and the model with all 2-factor interactions, and finally the independence model. To control for model fit we look at the corresponding deviances and degrees of freedom.

```
m4 <- loglin(table1, margin=list(c(1,2,3,4)), fit=TRUE)
cat("deviance(m4)=", m4$lrt, "df(m4)=", m4$df, "\n")

m3 <- loglin(table1, margin=list(c(1,2,3), c(1,2,4), c(1,3,4), c(2,3,4)), fit=TRUE)
cat("deviance(m3)=", m3$lrt, "df(m3)=", m3$df, "\n")

m2 <- loglin(table1, margin=list(c(1,2), c(1,3), c(1,4), c(2,3), c(2,4), c(3,4)),
              fit=TRUE)
cat("deviance(m2)=", m2$lrt, "df(m2)=", m2$df, "\n")

m1 <- loglin(table1, margin=list(c(1), c(2), c(3), c(4)), fit=TRUE)
cat("deviance(m1)=", m1$lrt, "df(m1)=", m1$df, "\n")
```

In order to see if a model or rather the reduction of a model is appropriate we use chi-square tests.

```

(df34 <- m3$df - m4$df)
(dev34 <- m3$lrt - m4$lrt)
1-pchisq(dev34, df34)

(df23 <- m2$df - m3$df)
(dev23 <- m2$lrt - m3$lrt)
1-pchisq(dev23, df23)

(df12 <- m1$df - m2$df)
(dev12 <- m1$lrt - m2$lrt)
1-pchisq(dev12, df12)

```

Since model "m2" fits the data well but model "m1" is definitely rejected we fit submodels of "m2" by leaving out one of the 2-factor interactions.

```

m2.GM <- loglin(table1, margin=list(c(1,3), c(1,4), c(2,3), c(2,4), c(3,4)),
  fit=TRUE)
cat("deviance(m2.GM)=", m2.GM$lrt, "df(m2.GM)=", m2.GM$df, "\n")

m2.MC <- loglin(table1, margin=list(c(1,2), c(1,3), c(1,4), c(2,4), c(3,4)),
  fit=TRUE)
cat("deviance(m2.MC)=", m2.MC$lrt, "df(m2.MC)=", m2.MC$df, "\n")

m2.CI <- loglin(table1, margin=list(c(1,2), c(1,3), c(1,4), c(2,3), c(2,4)),
  fit=TRUE)
cat("deviance(m2.CI)=", m2.CI$lrt, "df(m2.CI)=", m2.CI$df, "\n")

m2.GI <- loglin(table1, margin=list(c(1,2), c(1,3), c(2,3), c(2,4), c(3,4)),
  fit=TRUE)
cat("deviance(m2.GI)=", m2.GI$lrt, "df(m2.GI)=", m2.GI$df, "\n")

m2.GC <- loglin(table1, margin=list(c(1,2), c(1,4), c(2,3), c(2,4), c(3,4)),
  fit=TRUE)
cat("deviance(m2.GC)=", m2.GC$lrt, "df(m2.GC)=", m2.GC$df, "\n")

m2.MI <- loglin(table1, margin=list(c(1,2), c(1,3), c(1,4), c(2,3), c(3,4)),
  fit=TRUE)
cat("deviance(m2.MI)=", m2.MI$lrt, "df(m2.MI)=", m2.MI$df, "\n")

```

These six models all have 6 degrees of freedom so that the difference of degrees of freedom corresponding to model "m2" is 1 in each case.

```

1 - pchisq(m2.GM$lrt - m2$lrt, 1)

1 - pchisq(m2.MC$lrt - m2$lrt, 1)

1 - pchisq(m2.CI$lrt - m2$lrt, 1)

```

```

1 - pchisq(m2.GI$lrt - m2$lrt, 1)

1 - pchisq(m2.GC$lrt - m2$lrt, 1)

1 - pchisq(m2.MI$lrt - m2$lrt, 1)

```

Testing of the 2-factor interactions shows that the interactions "MC", "CI" and "MI" should be kept in the model. In the next step the model that contains these interactions, G—MC—MI—CI, is fitted.

```

m2.GM.GI.GC<- loglin(table1, margin=list(c(1), c(2,3), c(2,4), c(3,4)), fit=TRUE)
cat("deviance(m2.GM.GI.GC)=", m2.GM.GI.GC$lrt, "df(m2.GM.GI.GC)=", m2.GM.GI.GC$df,
    "\n")

1 - pchisq(m2.GM.GI.GC$lrt - m2$lrt, m2.GM.GI.GC$df - m2$df)

```

Comparison with model "m2" shows that reduction is possible. However, reduction to a model in which the main effect "G" is omitted is rejected.

```

m2.G<- loglin(table1, margin=list(c(2,3), c(2,4), c(3,4)), fit=TRUE)
cat("deviance(m2.G)=", m2.G$lrt, "df(m2.G)=", m2.G$df, "\n")

1 - pchisq(m2.G$lrt - m2$lrt, m2.G$df - m2$df)

```